## Cracking the Enigma: the Secret Battlefield of WW2



## October 15, 2022

## WW1 - first time radio was used in war

WW1 US Army portable radio station in Germany


Photo credit: US Army

US Army Code Book 1918

```
SECRET
M
    mbmorize this'group:
        "DAM..Code Lost."
        The
    "COLORADO"
        CODE
```

US Army Vigenère Disk 1912


TO SEND A MESSAGE
To oall a station make its call letter until ac-
knowledged, at intervals giving the oall or signal knowledged, at intervals giving the oall or signal
of the oalling station. If the oall letter of a station
is unknown, signal.- at intervals followed by the is unknown, signal. - at intervals followed by the
oall or signal of the oalling station until aoknowledged.
Make a slight pause after each letter and also after
 an error, he should make "A A front,", after whioh
he begins the word in which the error ooourred. and all were broken!

## Birth of crypto warfare

- Explosion of new cipher technology during WW1:
- One-time teletype tape
- Cipher wheel
- Strip cipher
- Burst encoder
- 4 electro-mechanical rotor machines:


Photo credit: Ralph Simpson, device at NCM. Ft. Meade, MD

Arthur Scherbius
Germany
1918


Photo credit: 1923 book, Technit, neue Apparate, Maschinen, Bauwerte


Photo credit: Bureau voor Industriele Eigendom

Arvid Damm
Sweden 1919


Photo credit: Austin Mills, device in NCM, Ft. Meade, MD

## Enigma invention - the classic story



## Arthur Scherbius

 Germany(1878-1929)


- Scherbius/Koch collaborated on Enigma, filed separate patents
- German Navy began testing Scherbius Enigma in 1926
- In 1927, Scherbius "curiously" bought the rights to Koch's patent, paid 600 Dutch guilders ( $\sim \$ 350$ )
" "Curious" because Scherbius owned the identical German patent
- Koch died in 1928; Scherbius in 1929 in a horse carriage accident
- Neither knew the role their invention would have in history


## History rewritten in 2003



Photo credit: Instituut voor Maritieme Historie, Den Haag

- 2003 bombshell: two Dutch naval officers invented the rotor cipher in 1915
- Patent attorney hired, but Dutch Navy suppressed patent during WW1
- Nov. 1919, Dutch Navy allowed naval officers patent, but Koch filed his patent 3 weeks earlier


Photo credit: Spengler family

- Naval officers filed lawsuit against Koch, but lost...
- They didn't know their patent attorney was Koch's brother-in-law!
- Judge was ex-Navy Minister who suppressed the patent in WW1!
- Now van Hengel and Spengler are recognized as the true inventors of the rotor cipher and the Enigma machine


## Dutch and German patents are exact copies

Dutch patent NL10700<br>filed 10/7/1919

- Dutch patent never built
- German patent was early version of Enigma
- Scherbius bought Dutch patent on 1/28/1927


Photo credit: Bureau voor Industriele Eigendom


## Birth of crypto warfare

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UPDA

- electro-mechanical rotor machines:


Photo credit: Bureau voor Industriele Eigendom

Edward Hebern USA
1917


Photo credit: Ralph Simpson, device in NCM. Ft. Meade, MD

Arvid Damm Sweden 1919


Photo credit: Austin Mills, device in NCM, Ft. Meade, MD

## Enigma machine



## Enigma machine - under the covers

- Typewriter style cipher machine, with light bulbs instead of printer
- Electro-mechanical rotors was the key innovation
- Rotors turn odometer style, so every letter in a message uses a different algorithm
- Reflector gives reciprocal encryption/decryption
- German military added plugboard



## Enigma wiring - animated!

## example: "A" enciphers/deciphers to "H"



## Cryptographic strength of Enigma

- Theoretical maximum \# of Enigma settings is $3 \times 10^{114}$ ( $\#$ atoms in universe $=10^{80}$ )
- If an enemy captures the Enigma, the \# settings is still astronomical - $10^{22}$
- $10^{22}$ is equal to a 75 bit key, far better than the 56 bit DES standard, used until 2001
- A 75 bit key means:

Webb Space Telescope view of cartwheel and spiral galaxies


Photo credit: NASA, ESA, CSA, STScl

If 100,000 Enigma operators could each check one key setting every second, 24X7...

It would take the age of the universe to break the code!

## Enigma Weaknesses



1. Greatest vulnerability was lax operator procedures
2. Reflector was reciprocal, so no letter encoded to itself
3. Rotors had regular, odometer movement
4. Ironically, brute strength of the Enigma gave Germans too much confidence in its security

Photo credit: Deutsches Bundesarchiv, colored by Lopatin V.

## Poland was first to break Enigma



Photo credit: Public domain, unknown photographer

- In 1932, German spy Hans-Thilo Schmidt sold Enigma keys to Allies
- Marian Rejewski used mathematics to recreate \& break Enigma, in Dec. 1932
- Breakthrough was breaking of rotors and plugboard separately, so now...
- 100,000 operators can break Enigma in 2 hours vs "twice age of universe"!
- Poles made "Bomba," 6 Enigmas in series, to quickly break daily key
(Bomba = Eureka in Polish)
- Polish codebreaking success kept secret for 7 years
- Poles finally disclosed Enigma secrets to UK and France just 5 weeks before Germany invaded Poland on Sept. 1, 1939


## British effort in breaking the Enigma

## Bletchley Park Mansion



Photo credit: Standardissuemagazine.com

- In 1939, UK began a major decoding effort at Bletchley Park, employing 11,000
- Effort led by Alan Turing, who built the Bombe: 36 Enigmas in series to find possible rotor settings
- After the Bombe found rotor settings, plugboard cables were solved manually


## Bombe - the beginning of computing



Photo credit: Godrey Argent Studio, via The Royal Society


Photo credit: NCM, Ft. Meade, "Solving the Enigma"

- Poles named their electro-mechanical codebreaker "Bomba," British used "Bombe" in honor of Polish contribution
- British exploited cribs vs Poles exploit of double message key
- 211 UK Bombes were built, most were destroyed after WW2
- US employed NCR to build a faster version of the Bombe to decode the 4-rotor naval Enigma - 121 were built


## Colossus computer



Photo credit: Ralph Simpson,
device at NCM, Ft. Meade, MD

- Colossus world's
- Uses 2400 vacuum anu
rable, digital computer
- Colossus breaks Lorenz teletype cipher, not Enigma
- Lorenz cipher used for high level messages


## U-boat peril

- Before the US entered the war, U-boats sank 60 ships/month
- U-boats roamed freely, then formed "wolfpacks" to sink convoys efficiently
- Nazis expected a UK blockade to result in a quick surrender
- Naval Enigma was initially the same as the Army, but later a 4-rotor version was used with more rigorous procedures
- Naval Enigma messages were secure until May 1941
> "The only thing that ever really frightened me during the wat was the U-boat peril."


## - Winston Churchill

U-boat sinks an English freighter, from a German book published during WWII


Photo credit: Naval History and Heritage Command

## Capture of U-110



Photo credit: reibert.info

- First code books captured from a U-boat was on May 9, 1941
- Captain died trying to scuttle U-110
- Germans didn't know 3 months of codes were stolen, by Lt. Balme
- 5 ships, from 1 Enigma message, were sunk on June 3 \& 4, 1941
- U-110 capture was the turning point in the Battle of the Atlantic

Lt. David Balme on deck of HMS Bulldog


Photo credit: forces.net

Balme leads boarding party to captured U-110


Photo credit: uboatarchive.net

## Battle of the Atlantic

- After breaking Naval Enigma, the British continuously re-routed convoys to avoid U-boats
- Unarmed weather trawlers carried Enigma, a recurring target for more code books
- British targeted supply ships and mother U-boats
- Early U-boat success turned to failure, 725 of

US bombing of U-117 - Aug. 1943


Photo credit: US National Archives 1155 U-boats and $82 \%$ of 35,000 sailors never returned from sea

- Some estimate breaking the Enigma shortened WW2 by 2 years


## Allied shipping losses vs codebreaking

Tons (000s)

## Allied Shipping Losses in WW2

## Did Germans know Enigma was broken?

- Allies only exploited Enigma messages after deception of traditional sources:
(spotter planes, spies, etc.)
- But, Allied codebreaking should have been suspected:
- 5 ships, from one Enigma message, all sunk in 2 days!


## Admiral Dönitz inspects U-boat

 at Saint-Nazaire, France

Photo credit: Bundesarchiv

- Supply convoy for Gen. Rommel in Africa found and sunk, despite continuous cloud cover from Naples to Africa
- Was 4-rotor Enigma designed to counter UK codebreaking?
- No, more likely security from other Nazi military or spies
- Confirmed in interview with Admiral Dönitz in 1974


## Enigma after WW2

- Codebreaking success was kept secret for 41 years, until 1974, despite thousands who knew the secret in the US and UK
- US and UK encouraged use of Enigma by other countries, including Allies, reading their secret messages for 3 decades
- About 35,000 Enigmas were manufactured
- Today, about 380 Enigma machines are known to exist, half in museums, half in private collections


David Hatch, NSA Historian, tells story of US Navy missile test, sinking "pallets" of Enigma machines
(pallet = 150 Enigmas = 2 tons)

Photo credit: US Navy release

## Enigma prices

## Enigma prices doubled after release of movie, "The Imitation Game" on Christmas, 2014

- In June 2017, a professor of cryptology found a "typewriter" in a Romanian flea market

Benedict Cumberbatch operates Enigma


Photo credit: StudioCana

- He knew it was an Enigma and bought it for 100 Euros
- Immediately sold on Romanian auction site for 45,000 Euros
- Sold 4 months later in US by Rau Antiques for $\$ 245,000$
- Rarity plus interest generate record prices at auction:
- \$441K for a 3-rotor Enigma at Sothebys on 4/30/21
- \$860K for a 4-rotor Enigma at Sothebys on 12/17/19


## Download this presentation

## CipherHistory.com/enigma.pptx

Cipher History Museum


## Addendum

## The following pages show the mathematics of the Enigma key space, both theoretically and as implemented by the Nazis

## Plugboard settings

- The German military addition of the plugboard added more key space than the rotors

- The \# of possible plugboard settings is a function of 3 variables:

1. \# plugboard cables, p, can be from 0 to 13
2. \# of groupings of possible plugged letters
(2p letters out of 26) = 26! / ((2p!) X (26-2p)!)
3. \# interconnections of letters within each group of plugged letters chosen from \#2 $=(2 p-1) X(2 p-3) X(2 p-5) X \ldots X 1$

- The 3 items above are calculated on the next slide


## Plugboard settings

$\left.\begin{array}{|c|r|r|r|}\hline \begin{array}{c}1 . \\ \text { \# plugboard } \\ \text { cables }\end{array} & \begin{array}{c}\text { 2. } \\ \text { \# groupings of } \\ \text { plugged letters } \\ 26!~ / ~((2 p!) ~ X ~(26-2 p)!) ~\end{array} & \begin{array}{c}\text { \# interconnections for each } \\ \text { set of plugged letters } \\ (2 p-1) \times(2 p-3) \times(2 p-5) \times \ldots \times 1\end{array} & \begin{array}{c}\text { Total \# } \\ \text { possible settings }\end{array} \\ \text { (column 2) X (column 3) }\end{array}\right)$

## Rotor settings

- The internal wiring of each rotor could be arranged in 26! different combinations. Since only 3 rotors are used, the number of combinations when selecting 3 unique rotors out of 26 ! is:

$$
\begin{aligned}
& \text { 26! X (26!-1) X }(26!-2)= \\
& 65,592,937,459,144,468, \\
& 297,405,473,480,371,753,615, \\
& 896,841,298,988,710,328,553, \\
& 805,190,043,271,168,000,000
\end{aligned}
$$

- Each of the 3 rotors could be set to any letter:
- $26 \times 26 \times 26=17,576$

- The rotors advance like an odometer, the setting to enable this is a notch set to any letter of the alphabet:
- $26 \times 26=676$ (Note: notch on left-most rotor has no effect)


## Reflector settings

- The reflector scrambles the letters in pairs so it could encrypt or decrypt with the same setting
- The letter "A" could be switched to any of the 25 remaining letters, the next letter could be switched to any of the 23 remaining letters, and so on
- Notice this result is the same
 as using 13 plugboard cables, since all letters are paired (see chart on page 23)

$$
\text { - } 25 \text { X } 23 \text { X } 21 \text { X ... X } 1=7,905,853,580,625
$$

## Total theoretical number of settings

- The total theoretical number of Enigma settings is thus the product of the 5 items on the previous 3 slides, or...
- 3,283,883,513,796,974,198,700,882,069,882,752,878, 379,955,261,095,623,685,444,055,315,226,006,433,615, 627,409,666,933,182,371,154,802,769,920,000,000,000
- Or $3.28 \times 10^{114}$
- This number is far greater than the total number of atoms in the observable universe $\left(10^{80}\right)$

Webb Space Telescope view of cartwheel and spiral galaxies


## Theory vs. practice

- The theoretical number of Enigma settings was not achieved in practice by the Germans, the number of settings the Allied Forces encountered for the standard 3-rotor Enigma:
- 10 plugboard cables were always used, reducing errors and the possible combinations to $150,738,274,937,250$
- Only 5 fixed rotors were issued out of 26! possibilities. Since the wiring was known, selecting 3 out of 5 is $5 \times 4 \times 3=60$
- The initial settings of the rotors and the positions of the notches remain the same at 17,576 and 676
- Reflector setting was known and remained unchanged = 1
- The product of the above numbers is: $107,458,687,327,250,619,360,000$ or $1.07 \times 10^{23}$
- $1.07 \times 10^{23}$ is equivalent to a 76 bit key, better than 56 bit DES, the first PC standard in use until 2001


## Enigma codebreaking example

- Germans considered the Enigma to be unbreakable
- Before computers, a brute force attack was impossible:
- To test $10^{23}$ key settings:


## If 100,000 Enigma operators could each check one key setting every second, 24X7... <br> It would take twice the age of the universe to break the code!

- Each U-boat, Air Force, and Army unit had separate keys, which changed daily!
- The British Bombe did not perform brute force attacks but searched for possible cribs to decode the rotors only
- The plugboard, which gave more key space than the rotors, was manually, and easily, decoded

